



Asignatura: Criptografía
Código: 30076
Centro: Ciencias
Titulación: Máster en Matemáticas y aplicaciones
Nivel: Máster M2
Tipo: Optativa
Nº de créditos: 8

ASIGNATURA / **COURSE TITLE**

Cryptography

1.1. Código / **Course number**

30076

1.2. Materia / **Content area**

Cryptography

1.3. Tipo / **Course type**

Elective subject.

1.4. Nivel / **Course level**

Master M2

1.5. Curso / **Year**

2011/2012

1.6. Semestre / **Semester**

2nd (Spring semester)

1.7. Número de créditos / **Credit allotment**

8 ECTS credits

1.8. Requisitos previos / **Prerequisites**

We assume as a prerequisite for this course a basic proficiency in elementary number theory and group theory. Some knowledge of algebraic curves is useful. Key results will be recalled in the course. For the programming projects prior experience with computers is assumed. Projects will be handled using mostly Sage, but other computing languages are acceptable.

1.9. Requisitos mínimos de asistencia a las sesiones presenciales / **Minimum attendance requirement**

75%



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1.10. Datos del equipo docente / Faculty data

Docente(s) / Lecturer(s): [Adolfo Quiros Gracián](#)
Departamento de / Department of: [Mathematics](#)
Facultad / Faculty: [Science](#)
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Horario de atención al alumnado/Office hours: [By appointment](#)

1.11. Objetivos del curso / Course objectives

In this course we present some of the mathematical techniques employed in public-key cryptography. We consider RSA, ElGamal and elliptic curve cryptosystems. This latter is one of the most serious competitors to RSA cryptosystem and deeper from the mathematical point of view.

1.12. Contenidos del programa / Course contents

1. **Historical introduction.** Motivation and examples. Elementary group theory and number theory. Finite fields. Simple encryption algorithms.
2. **The RSA cryptosystem.** Algorithm, examples and cautions. Primality tests and factorization algorithms. Introduction to the number field sieve.
3. **Discrete logarithm problem.** Statement and examples. Basic attacks. Diffie-Hellman key exchange. The ElGamal cryptosystem.
4. **Elliptic curve cryptography.** Elliptic curves and group law. Elliptic curves and factorization. The elliptic version of the discrete logarithm problem. Pairings and cryptography.
5. **Complementary topics.** Digital signatures. The DES and AES algorithms. Knapsack cryptosystems.

1.13. Referencias de consulta / Course bibliography

- [1] Blake, I. F.; Seroussi, G.; Smart, N.P. Elliptic curves in cryptography. Reprint of the 1999 original. London Mathematical Society Lecture Note Series, 265. Cambridge University Press, Cambridge, 2000.
- [2] Koblitz, N. A course in number theory and cryptography. Second edition. Graduate Texts in Mathematics, 114. Springer-Verlag, New York, 1994.
- [3] Koblitz, N. Algebraic aspects of cryptography, Springer-Verlag, New York, 1998
- [4] J. Menezes, P. C. van Oorschot, S. A. Vanstone. Handbook of applied cryptography, CRC Press (1997). [<http://www.cacr.math.uwaterloo.ca/hac/>]
- [5] Stein, W. Elementary number theory: primes, congruences, and secrets. A computational approach. Undergraduate Texts in Mathematics. Springer, New York, 2009.
- [6] D. R. Stinson. Cryptography theory and practice. Chapman & Hall/CRC (2006)



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2. Métodos Docentes / **Teaching methodology**

The lectures combine theoretical and practical aspect. We shall try to use the computer. However, taking into account that the course is devoted to mathematical aspects of cryptography, the purpose of the programming exercises will be to understand the theoretical basis rather than to design actual efficient applications. There will be programmed tutoring sessions.

3. Tiempo de trabajo del estudiante / **Student workload**

		Nº de horas	Porcentaje
Presencial	Clases teóricas	42h (21%)	66 h (33%)
	Clases prácticas	4h (2%)	
	Tutorías	14h (7%)	
	Seminarios y trabajos	4h (2%)	
	Examen final / proyecto	2h (1%)	
No presencial	Elaboración de problemas	40h (20%)	134 h (67%)
	Estudio semanal	88h (44%)	
	Preparación de examen (presentación)	6h (3%)	
Carga total de horas de trabajo: 25 horas x 8 ECTS		200h	

4. Métodos de evaluación y porcentaje en la calificación final / **Evaluation procedures and weight of components in the final grade**

- 1) Final exam and/or final project: 50%.
- 2) Exercises and computer assignments: 40%.
- 3) In-class exercises, participation: 10%

EVALUACIÓN EXTRAORDINARIA / Make up exam: Examen ante tribunal de Máster / examination by a committee



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5. Cronograma* / Course calendar

Semana Week	Contenido Contents	Horas presenciales Contact hours	Horas no presenciales Independent study time
1-2	Historical introduction	6	12
2-5	Discrete logarithm problem	12	24
5-8	The RSA cryptosystem	12	24
8-12	Elliptic curve cryptography	16	32
12-14	Complementary topics	10	20
15-16	Evaluation	10	22

*This calendar is tentative.