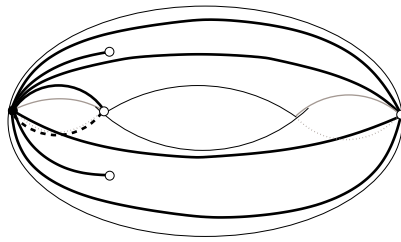


Riemann surfaces and dessins d'enfants

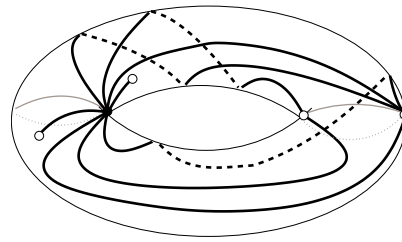
A Riemann surface is simply a surface endowed with an atlas in which the transition functions are holomorphic.

The theory of compact Riemann surfaces is a meeting point for topology, geometry and algebra. This is because compact Riemann surfaces can be regarded as complex irreducible curves “ $F(x, y) = \sum a_{ij}x^i y^j = 0$ ”, and, moreover, the case in which the coefficients a_{ij} are algebraic numbers corresponds to certain simple graphs embedded in a compact oriented topological surface called dessins d'enfants (Grothendieck's-Belyi theory of dessins).

$$y^2 = x(x-1)(x-\sqrt{2})$$



$$y^2 = x(x-1)(x+\sqrt{2})$$



Bibliography

1. G. Belyi. On Galois extensions of a maximal cyclotomic field, Math, USSR Izv. 14, No.2 (1980), 247-256.
2. E. Girono, G. Gonzalez-Diez. Introduction to compact Riemann surfaces and dessins d'enfants. London Mathematical Society Student Texts, 79 Cambridge University Press, Cambridge, 2012. xii+298 pp. ISBN: 978-0-521-74022-7
10. A. Grothendieck. Esquisse dun Programme. London. Math. Soc, L.N.Series 242. (L.Schneps and P. Lochak, editors)